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## INTRODUCTION

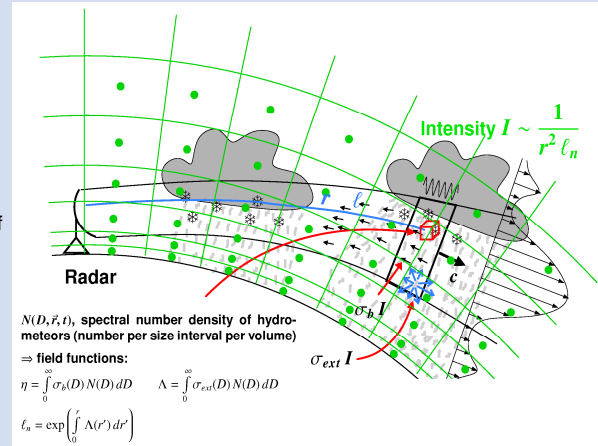
A new radar forward operator for simulating terrestrial weather radar measurements (reflectivity  $Z_e$ , radial wind  $v_r$ ) from NWP model output has been developed within an Extramural Research project. It is suitable for a broad range of applications like, e.g., **radar data assimilation in the framework of Ensemble Kalman Filter systems** (such as the KENDA system) or **verification of cloud microphysical parameterizations**. The operator comprises all relevant physical aspects of radar cloud measurements in a quite accurate way, but at the same time providing the possibility for simplifications in a modular fashion to gain efficiency at the expense of accuracy. **Main design criteria: efficiency, applicability on supercomputers, parallel and vectorizable code.**

## RADAR FORWARD OPERATOR AND NWP MODEL

**Basic purpose of forward operator:** simulate the measurement process of radar observables like radial wind  $v_r$  or equiv. reflect. factor  $Z_e$  within the „virtual reality“ of an NWP model.

**Main ingredients (as depicted to the right):**

- Green: model grid boxes = native grid for the modeled hydrometeor variables,  $u, v, w, T, p, e$ .
- Beam propagation, depends on refractive index of air (function of  $T, p, e$ ).
- Effective beam weighting function / pulse volume.
- Backscattering / extinction: field functions  $\eta, \Lambda$ .
- Compute  $\eta, \Lambda$  and  $v_r$  from model variables on model grid (Mie-scattering or Rayleigh), then interpolate to (sub-)beams of the „radar“ grid and apply radar forward operator equations below.



## BASIC EQUATIONS FOR $Z_e$ AND $v_r$ (POLARISATION PARAMETERS OMITTED)

**Radar operator for equivalent reflectivity factor  $Z_e$  in "beam system", single beam:**

$$Z_e^{(R)}(r_0) = \frac{\int_{r_0-ct/4}^{r_0+ct/4} \int_{-\pi/2}^{\pi/2} \int_{-\pi/2}^{\pi/2} Z_e(r, \phi, \theta) \exp\left(-2 \int_0^r \Lambda(r', \phi, \theta) dr'\right) \frac{f^4(\phi, \theta)}{r^2} \cos \theta d\theta d\phi dr}{\int_{r_0-ct/4}^{r_0+ct/4} \int_{-\pi/2}^{\pi/2} \int_{-\pi/2}^{\pi/2} \frac{f^4(\phi, \theta)}{r^2} \cos \theta d\theta d\phi dr}$$

with  $l_n^{-1}$  = path integrated attenuation by precip from the radar to location  $(r, \phi, \theta)$ .

**Radar operator for radial velocity in "beam system", single beam:**

$$v_r^{(R)}(r_0) = \frac{\int_{r_0-ct/4}^{r_0+ct/4} \int_{-\pi/2}^{\pi/2} \int_{-\pi/2}^{\pi/2} (\hat{v} \cdot \hat{z}_r) \frac{\eta}{\rho_a} \frac{f^4}{r^2} \cos \theta d\theta d\phi dr}{\int_{r_0-ct/4}^{r_0+ct/4} \int_{-\pi/2}^{\pi/2} \int_{-\pi/2}^{\pi/2} \frac{\eta}{\rho_a} \frac{f^4}{r^2} \cos \theta d\theta d\phi dr} - \frac{\int_{r_0-ct/4}^{r_0+ct/4} \int_{-\pi/2}^{\pi/2} \int_{-\pi/2}^{\pi/2} (\hat{z}_b \cdot \hat{z}_r) \bar{v}_r \frac{\eta}{\rho_a} \frac{f^4}{r^2} \cos \theta d\theta d\phi dr}{\int_{r_0-ct/4}^{r_0+ct/4} \int_{-\pi/2}^{\pi/2} \int_{-\pi/2}^{\pi/2} \frac{\eta}{\rho_a} \frac{f^4}{r^2} \cos \theta d\theta d\phi dr}$$

Above,  $Z_e$  and the reflectivity weighted hydrometeor fallspeed  $\bar{v}_r$  are defined as

$$Z_e(r, \phi, \theta) = \eta(r, \phi, \theta) \frac{\lambda^4}{\pi^5 |\mathbf{K}_{w,0}|^2} \quad \bar{v}_r = \frac{1}{\eta} \int_0^\infty \sigma_b(D) N(D) v_r(D) dD$$

**Actually implemented: Radar operator for  $Z_e$  in "radar system", assuming azimuthal averaging of successive pulses, disregarding range weighting:**

$$\langle Z_e^{(R)} \rangle(r_0, \alpha_0, \epsilon_0) = \frac{\int_{\alpha_0-\pi}^{\alpha_0+\pi} \int_{\epsilon_0-\pi/2}^{\epsilon_0+\pi/2} Z_e(r_0, \alpha, \epsilon) \exp\left(-2 \int_0^{r_0} \Lambda(r', \alpha, \epsilon) dr'\right) \frac{f_e^4(\alpha, \epsilon)}{r_0^2} \cos \epsilon d\epsilon d\alpha}{\int_{\alpha_0-\pi}^{\alpha_0+\pi} \int_{\epsilon_0-\pi/2}^{\epsilon_0+\pi/2} \frac{f_e^4(\alpha, \epsilon)}{r_0^2} \cos \epsilon d\epsilon d\alpha}$$

with the approximate effective beam weighting function of an azimuthally scanning radar (Blahak, 2008):

$$f_e^4(\alpha, \epsilon) = \exp\left\{-8 \ln 2 \left[ \left( \frac{(\alpha - \alpha_0) \cos \epsilon}{\sigma_{3,eff0} + (\cos \epsilon_0 - 1) \Delta \alpha (1 - \exp(-1.5 \Delta \alpha / \theta_3))} \right)^2 + \left( \frac{\epsilon - \epsilon_0}{\theta_3} \right)^2 \right] \right\}$$

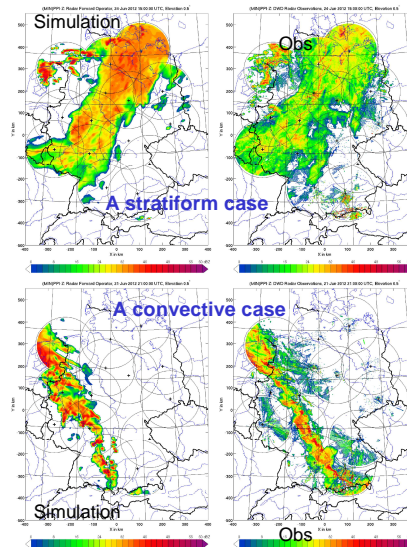
**Neglections:** range weighting; radar miscalibration; wet radome attenuation; gaseous attenuation; aliasing

**Possible (modular) simplifications:** disregard horizontal / vertical smoothing; disregard reflectivity weighting / hydrometeor fallspeed for  $v_r$ ; Rayleigh instead of Mie; disregard hydrometeor attenuation; offline or online beam propagation (Zeng et al., 2013)

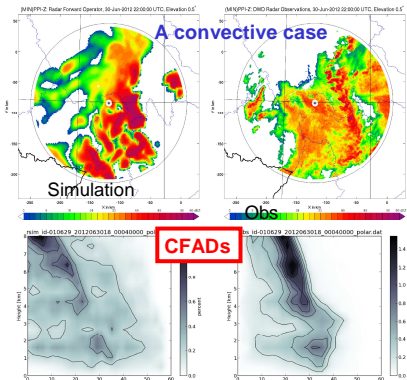
Literature: Blahak, 2008: An approximation to the effective beam weighting function for scanning meteorological radars, JAOTECH  
Blahak, 2007: RADAR\_MIE\_LM and RADAR\_MIELIB - calculation of radar reflectivity from model output, Internal Report  
Zeng et al., 2013: Radar beam tracing methods based on atmospheric refractive index, JAOTECH, submitted

## MODEL VERIFICATION

Examples of case studies: COSMO-DE with simulations and observations of 16 German radars every 15 min, shown as PPI-overlays:



Good way to compare Sim and OBS: CFADs (Contoured Frequency by Altitude Diagrams)



## FIRST ASSIMILATION EXPERIMENTS

- 17 C-Band dual polarisation Doppler radars
- COSMO-DE Ensemble of 40 Members, driven by GME global test ensemble
- First experiment for mainly technical tests: 31.5.2011, 18 UTC + 03 h
- Assimilate radial wind every hour by LETKF using the KENDA Software
- **Results for v-component after third assimilation cycle for different localization radii:** fg (mean) | assim. incr. (mean) | fg (spread)

