#### Spatial non-homogeneous Gaussian regression

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## Statistical postprocessing



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# Motivation spatial postprocessing

state-of-the-art ensemble postprocessing methods:

- Bayesian model averaging (BMA)
- non-homogeneous Gaussian regression (NGR), also known as ensemble output statistics (EMOS)

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BUT: ignore spatial correlation between different observation

## Forecast Fields

Assuming the forecast uncertainties at different sites are independent, then samples of the predictive distribution look like this:



## Forecast Fields

We present a statistical postprocessing method which models spatially consistent temperature forecast fields:



Spatial non-homogeneous Gaussian regression - Overview

combination of non-homogeneous Gaussian regression and the geostatistical output perturbation method (GOP)

| NGR               | GOP           |  |
|-------------------|---------------|--|
| for ensemble      | one member    |  |
| independent sites | weather field |  |

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 $\Rightarrow$  spatial NGR

- uses full information of ensemble
- models spatial correlation

# Part 1: Non-homogeneous Gaussian regression

- proposed by Gneiting et al., 2007
- applicable to different weather variables, such as temperature, wind speed, precipitation
- yields full predictive distribution
- distribution characteristics are modeled as functions of the ensemble information
- assumption: the forecast error on the verfication day behaves similar to the forecast errors on the *n* previous days

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#### Part 1: NGR for temperature

$$y_s|f_{1s},...,f_{Ms} \sim \mathcal{N}(a_1 + b_1f_{1s} + ... + b_Mf_{Ms}, c + dS_s^2),$$



#### where

- $y_s$  temperature at location s
- *f*<sub>1s</sub>, ..., *f*<sub>Ms</sub> ensemble forecasts for location s

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- S ensemble variance
- *a*, *b*<sub>1</sub>, ..., *b*<sub>M</sub> bias-correcting parameters
- c, d spread parameters

Part 2: Geostatistical output perturbation method

- proposed by Gel et al., 2004
- models forecast errors with a Gaussian random field (GRF)

#### $\mathbf{Y}|\mathbf{F} = a\mathbf{1} + b\mathbf{F} + \mathbf{E}_1 + \mathbf{E}_2$

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#### where

- Y temperature field
- F forecast field of one member
- **E**<sub>1</sub> continuous error field
- **E**<sub>2</sub> discontinuous error field
- *a*, *b* bias-correcting parameter

# Combination of NGR and GOP

- fit NGR model as before
- 2 calculate standardized forecast errors during the training period

$$\frac{y_s - (a + b_1 f_{s1} + ... + b_M f_{sM})}{\sqrt{c + dS^2}}, \ s \in S$$

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- estimate covariance function of GRF based on forecast errors
- simulate forecast errors according to this GRF and scale them
- add them to the means of the predictive distributions

# COSMO-DE-EPS

- temperature forecasts
- time period: 10 December 2010 to 30 November 2011
- lead time: 21hours
- initialization time: 00:00UTC
- observations at 514 SYNOP stations



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# Verification Results: overall

If verified individually, the scores for NGR and spatial NGR coincide.

| Model        | CRPS | MAE  |
|--------------|------|------|
| Raw ensemble | 1.57 | 1.77 |
| NGR          | 1.04 | 1.46 |
| Spatial NGR  | 1.04 | 1.46 |



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## Verification results: minimum temperature along A3

17 SYNOP stations at a section of A3 between Frankfurt and Cologne

| Model        | CRPS | MAE  |
|--------------|------|------|
| Raw ensemble | 1.72 | 1.92 |
| NGR          | 1.05 | 1.37 |
| Spatial NGR  | 0.86 | 1.20 |



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Verification results: minimum temperature along A3

Application: winter road maintenance

- salt the road if temperatures are predicted to drop below zero somewhere on the considered section of the A3
- otherwise don't salt

considering winter months of January, February and November 2011

| Model        | Brier score |  |
|--------------|-------------|--|
| Raw ensemble | 0.120       |  |
| NGR          | 0.114       |  |
| Spatial NGR  | 0.083       |  |

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#### Verification Results: average temperature

prediction of average temperature in 14 of Germany's states

| Model        | CRPS | MAE  |
|--------------|------|------|
| Raw ensemble | 1.26 | 1.43 |
| NGR          | 0.85 | 1.00 |
| spatial NGR  | 0.71 | 0.95 |



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# Summary

- importance of spatial modeling, especially when considering minima, maxima, totals or averages
- spatial NGR is a method which generates spatially consistent temperature fields
- case study: spatial NGR superior to raw ensemble as well as NGR

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# Thank you for your attention!

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